

1 Discussion Pre-Check

- 1.1 True or False: The idea of floating point is to use the ability to move the radix (decimal) point wherever to represent a large range of real numbers as exact as possible.
- 1.2 True or False: Floating Point and Two's Complement can represent the same total amount of numbers (any reals, integer, etc.) given the same number of bits.
- 1.3 True or False: The distance between floating point numbers increases as the absolute value of the numbers increase.
- 1.4 True or False: Floating Point addition is associative.
- 1.5 Why does normalized scientific notation always start with a 1 in base-2?
- 1.6 Convert the following numbers into the quantity of bytes each term represents (you may leave your answer in terms of powers of 2). (See precheck section on IEC Prefixes for assistance)
- a) 4 KiB
- b) 2 MiB

2 *Precheck: C, Floating Point, IEC*

c) 8 Kib

d) 24 GiB

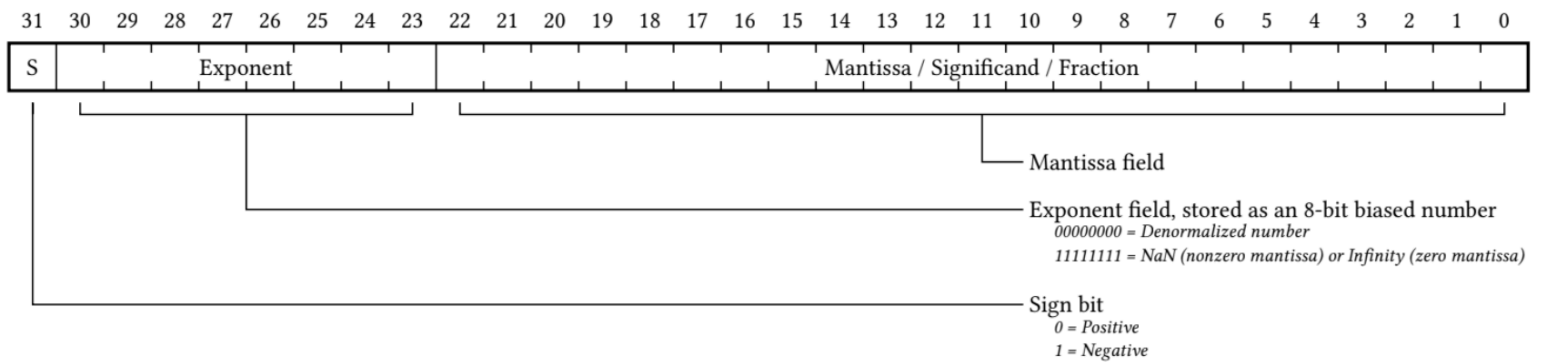
e) 19 TiB

2 Floating Point

The IEEE 754 standard defines a binary representation for floating point values using three fields.

- The *sign* determines the sign of the number (0 for positive, 1 for negative).
- The *exponent* is in **biased notation**. For instance, the bias is 127, which comes from $(2^{\{8-1\}} - 1)$ for single-precision floating point numbers. For double-precision floating point numbers, the bias is 1023
- The *significand* (or *mantissa*) is akin to unsigned integers but used to store a fraction instead of an integer and refers to the bits to the right of the leading “1” when normalized. For example, the significand of 1.010011 is 010011.

The table below shows the bit breakdown for the single-precision (32-bit) representation. The leftmost bit is the MSB, and the rightmost bit is the LSB.



For normalized floats:

$$\text{Value} = (-1)^{\text{Sign}} \times 2^{\text{Exp}-\text{Bias}} \times 1.\text{Significand}_2$$

For denormalized floats:

$$\text{Value} = (-1)^{\text{Sign}} \times 2^{\text{Exp}-\text{Bias}+1} \times 0.\text{Significand}_2$$

Exponent (Pre-bias)	Significand	Meaning
0	Anything	Denorm
1-254	Anything	Normal
255	0	$\pm$ Infinity
255	Nonzero	NaN

Note that in the above table, our exponent has values from 0 to 255. When translating between binary and decimal floating point values, we must remember that there is a bias for the exponent.

3 IEC Prefixes and Symbols

IEC Prefix multipliers are a set of standard units used to represent powers of 2 and are often used in discussion about caches and memory. The Base-2 (bi: “bee”) IEC standard prefixes represent binary quantities officially up to exbi (“exbee”). Their comparison to SI units are shown below:

Prefix (Abbr)	SI Size
Kilo (k)	$10^3 = 1,000$
Mega (M)	$10^6 = 1,000,000$
Giga (G)	$10^9 = 1,000,000,000$
Tera (T)	$10^{12} = 1,000,000,000,000$
Peta (P)	$10^{15} = 1,000,000,000,000,000$
Exa (E)	$10^{18} = 1,000,000,000,000,000,000$
Zetta (Z)	$10^{21} = 1,000,000,000,000,000,000,000$
Yotta (Y)	$10^{24} = 1,000,000,000,000,000,000,000,000$

IEC (Abbr)	IEC Factor
Kibi (Ki)	$2^{10} = 1,024$
Mebi (Mi)	$2^{20} = 1,048,576$
Gibi (Gi)	$2^{30} = 1,073,741,824$
Tebi (Ti)	$2^{40} = 1,099,511,627,776$
Pebi (Pi)	$2^{50} = 1,125,899,906,842,624$
Exbi (Ei)	$2^{60} = 1,152,921,504,606,846,976$
Zebi (Zi)	$2^{70} = 1,180,591,620,717,411,303,424$
Yobi (Yi)	$2^{80} = 1,208,925,819,614,629,174,706,176$